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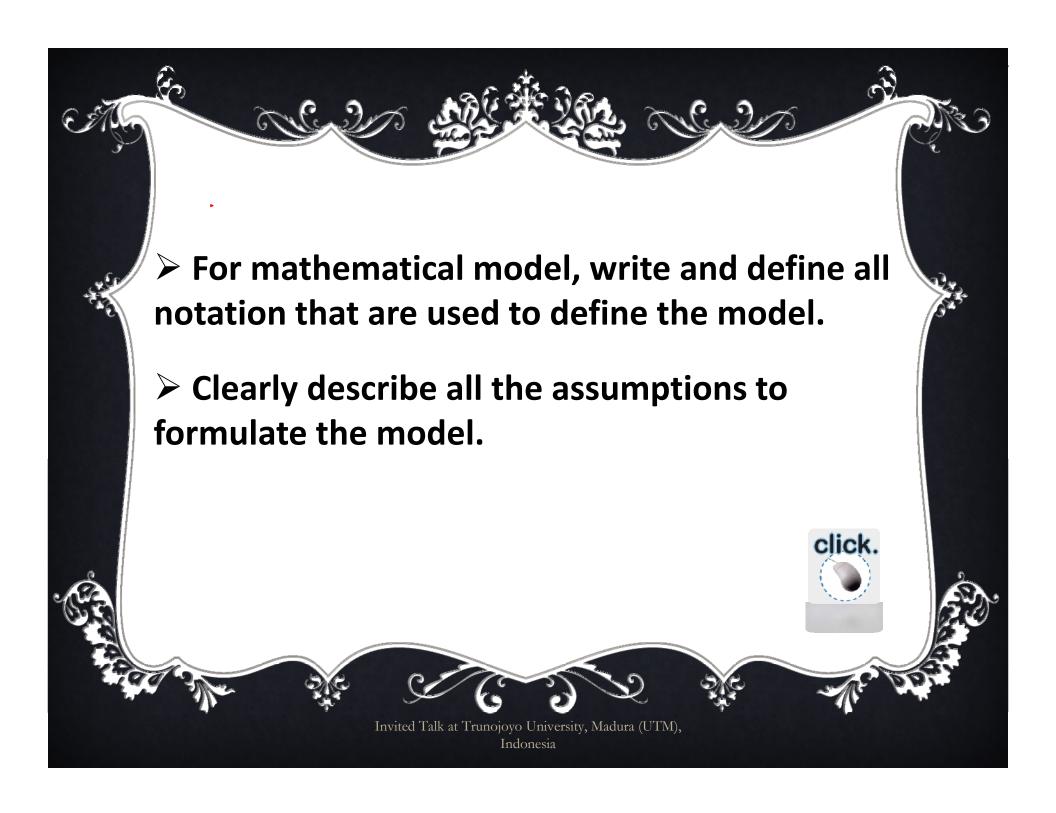
The symbol * represents the corresponding author

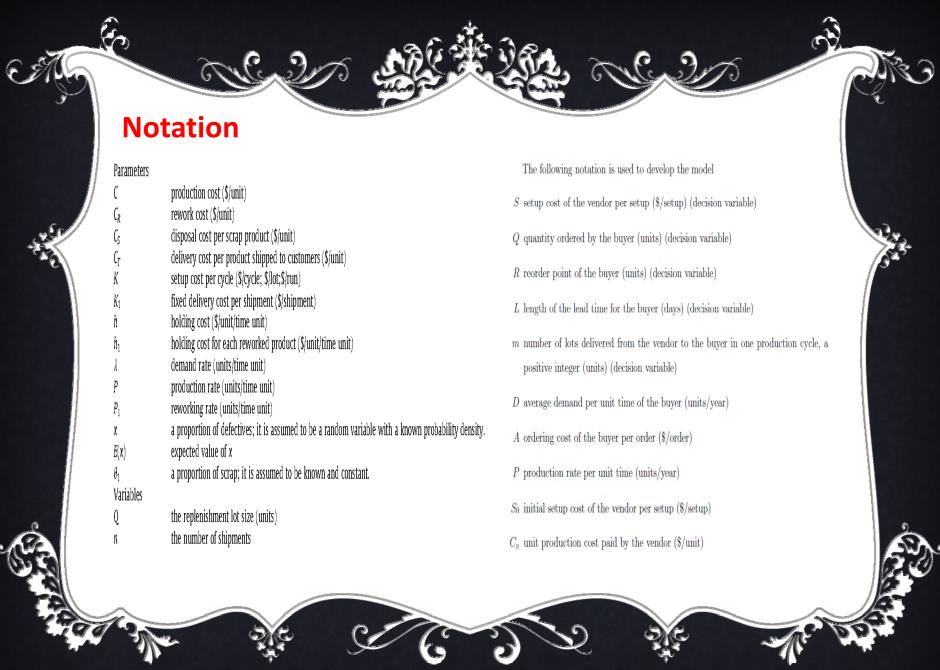
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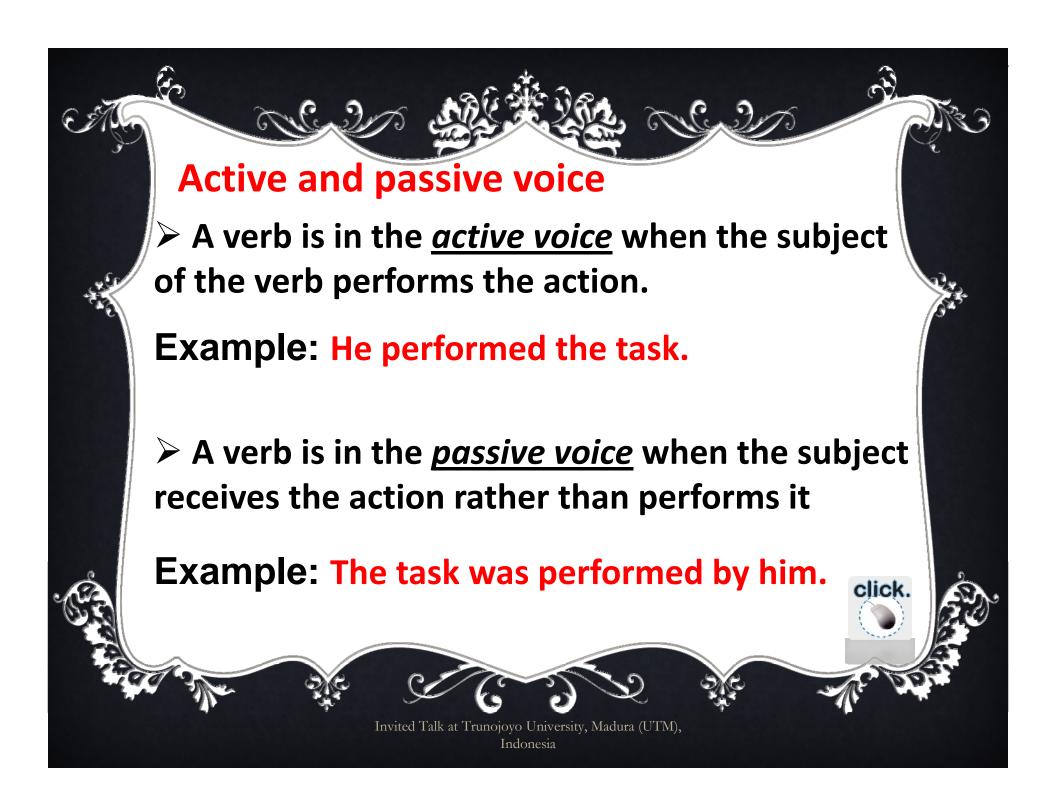
Invited Talk at Trunojoyo University, Madura (UTM), Indonesia

Assumptions

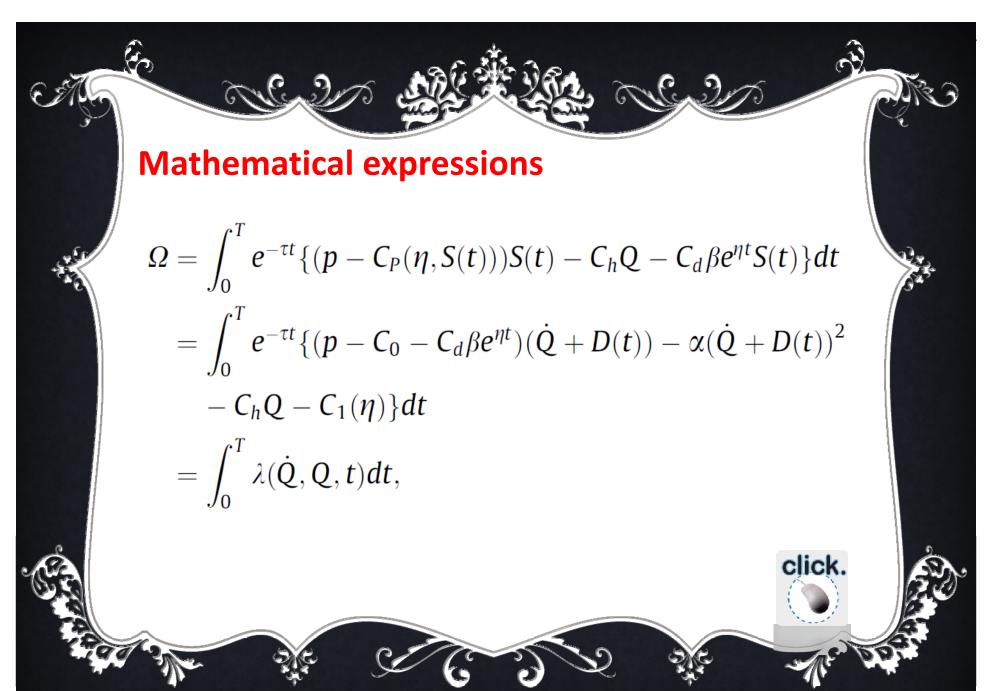
- 1 The deterioration function $\phi(t)$ depends on time as $\phi(t) = \gamma t$, where γ is a constant $(0 < \gamma \le 1, t \ge 0)$.
- 2 Within the time interval $[0,t_d]$, the product has no deterioration. Deterioration occurs within the time interval $[t_d,t_1]$ at a variable deterioration rate $\phi(t)$.
- 3 $I_1(t)$ denotes the inventory level at any time $t \in [0,t_d]$ without the deterioration of product. $I_2(t)$ stands for the inventory level at any time $t \in [t_d,t_1]$ with the product deterioration. $I_3(t)$ signifies the inventory level at any time $t \in [t_1,T]$ with the product shortage.
- 4 The demand rate D(I(t)) is known as a function of instantaneous stock level I(t); D(I(t)) is taken as following form:

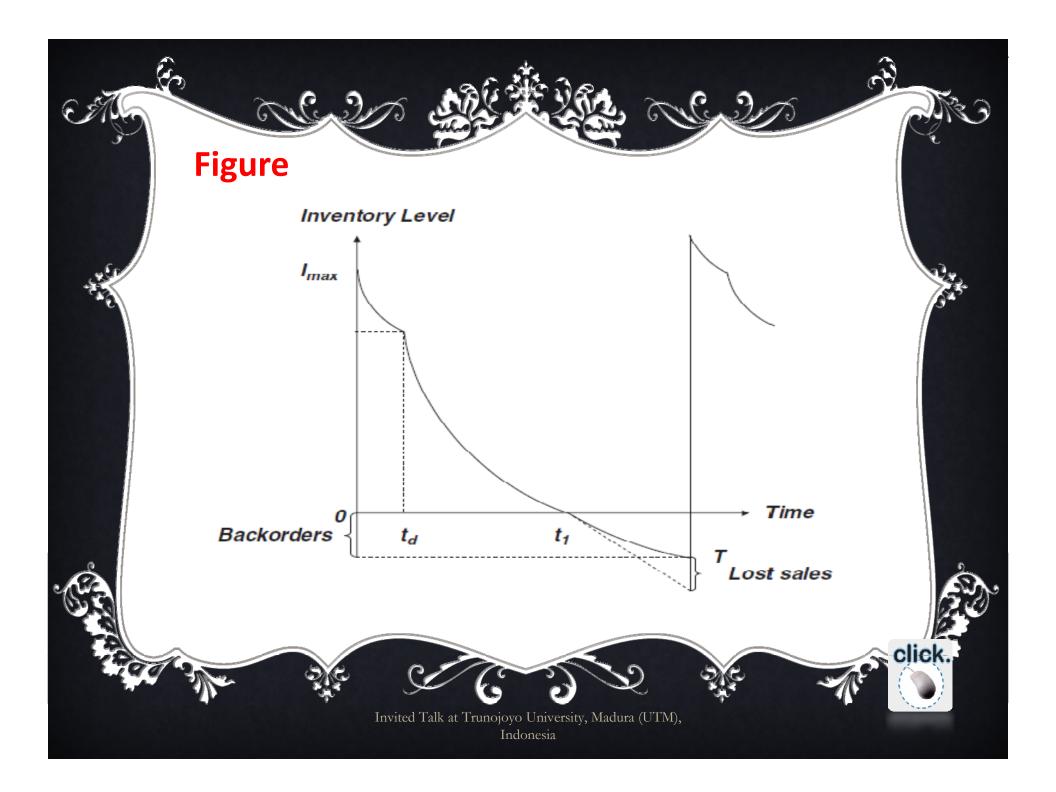
$$D(I(t)) = \begin{cases} \alpha + \beta I(t) & \text{if } i(t) > 0, \\ \alpha & \text{if } i(t) \leq 0. \end{cases}$$

- 5 Shortages as well as backlogging are allowed. It is considered that only a fraction of demand is backlogged, we denote it $B(t) = \frac{1}{1+\varepsilon t}$, where t is the waiting time and $\varepsilon > 0$ is a constant backlogging parameter.
- 6 Replenishment rate is infinite and lead time is negligible.
- 7 A single type of item is considered in this model.







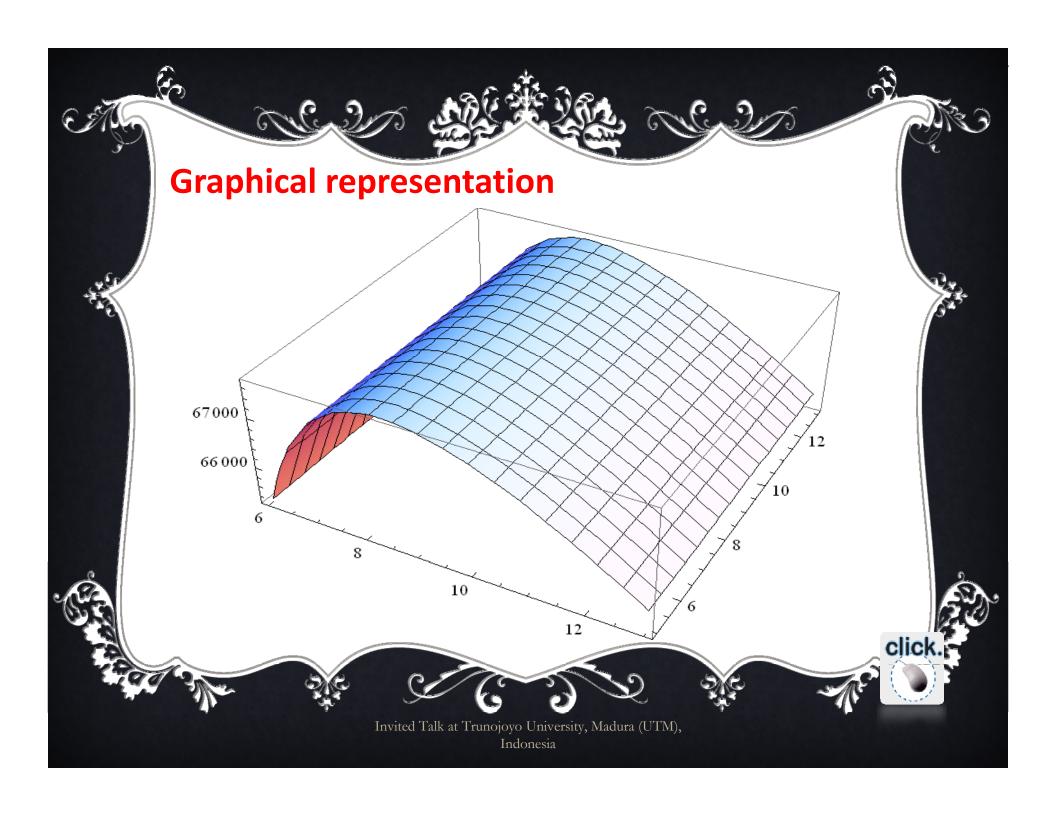


Numerical data Lead time Unit crashing Minimum Normal duration duration cost component b_i (days) a_i (days) c_i (\$/day) 20 0.4 20 1.2 16 5.0



Numerical results

m	L_m^{*a}	$R_m^*(k_m^*)$	Q_m^*	$\mathrm{JTEC_N}(Q_m^*, R_m^*, L_m^*, m)$
1	28	58 (0.84)	299	\$7466.7
2	28	62 (1.14)	189	\$6760.0
3	28	64 (1.31)	144	\$6660.4← ^b
4	28	66 (1.41)	118	\$6722.5



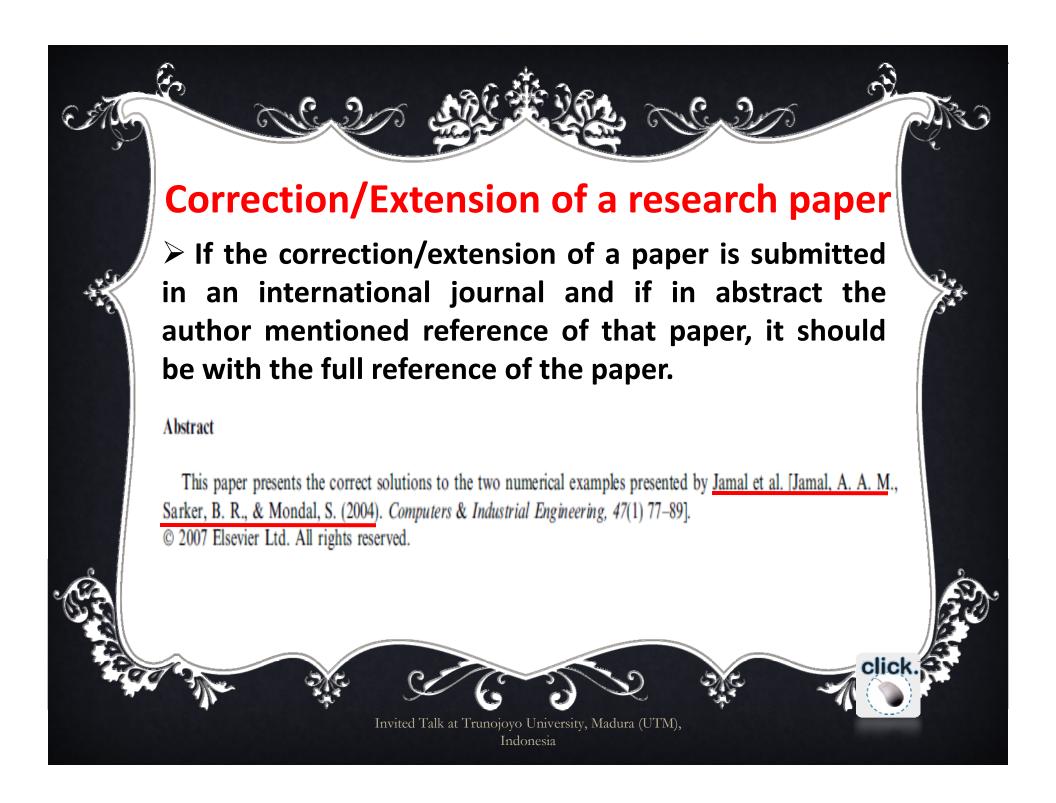


Comparison table

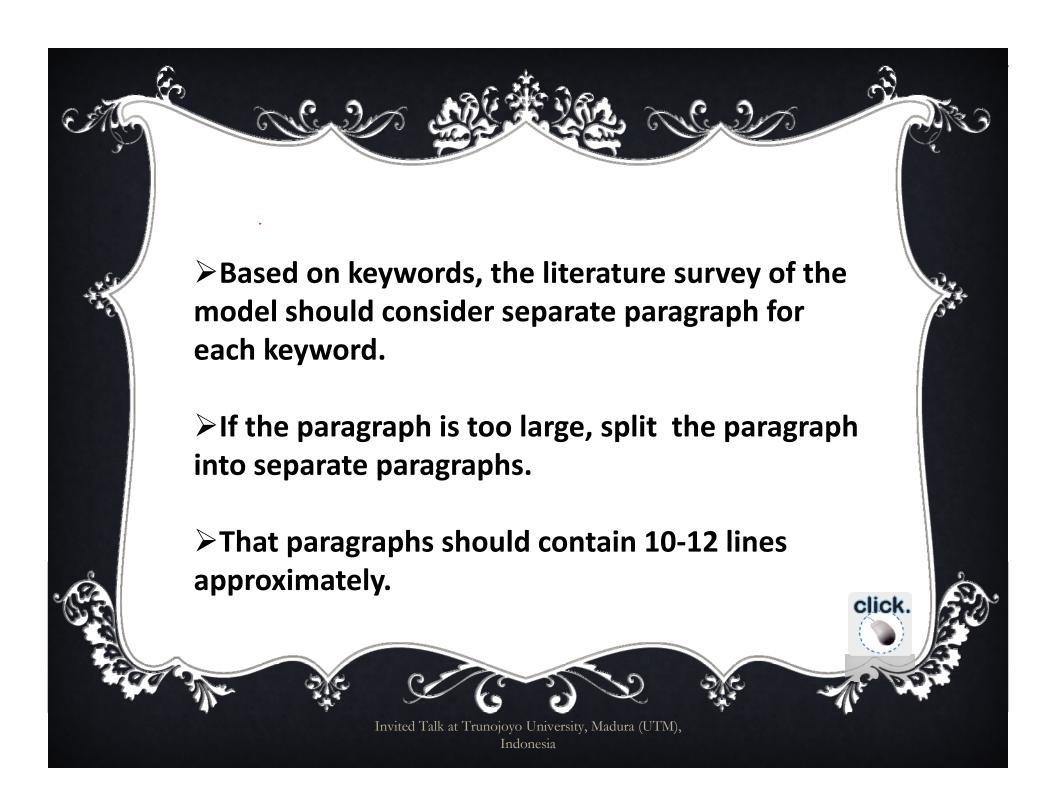
Comparison table (for m > 1)

	Goyal [7]	Ouyang et al. [25]	This model
Number of lots delivered (m)	2	3	3
Reorder point (R) (units)	_	64	65
Buyer's ordering quantity (Q) (units)	164	144	134
Vendor's lot size (mQ) (units)	328	432	402
JATC (\$)	7875.1	6660.4	6627.4

- indicates the reorder point was not considered as a decision variable in Goyal [7].





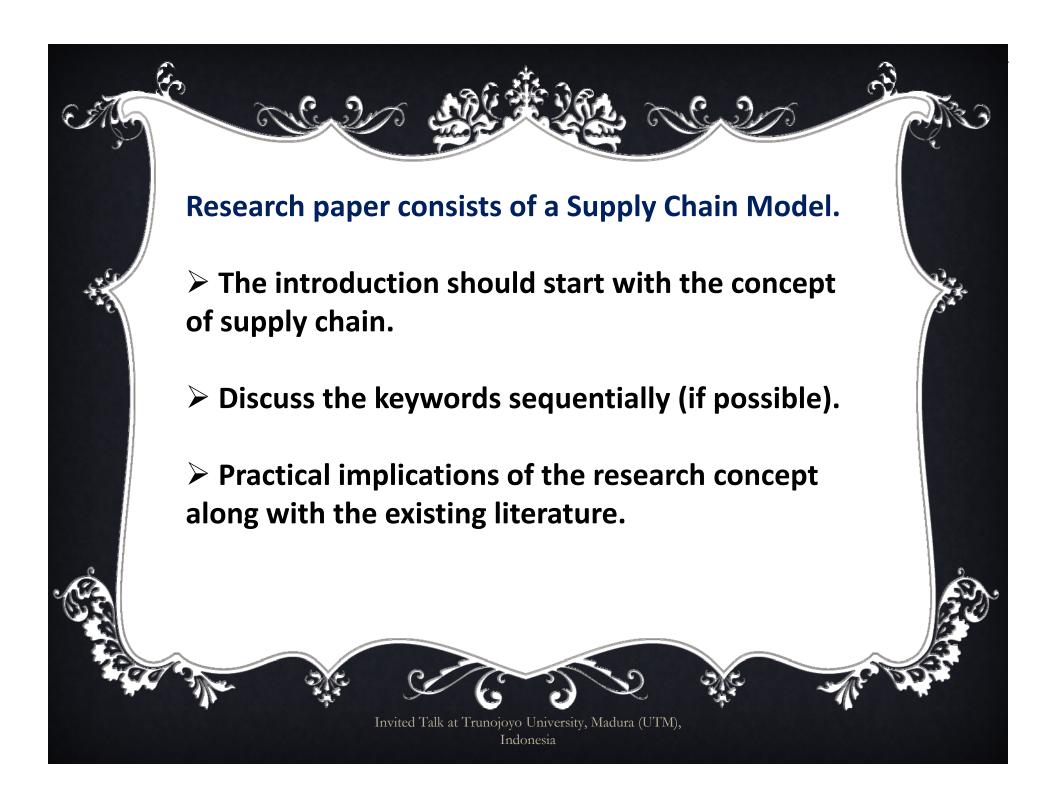


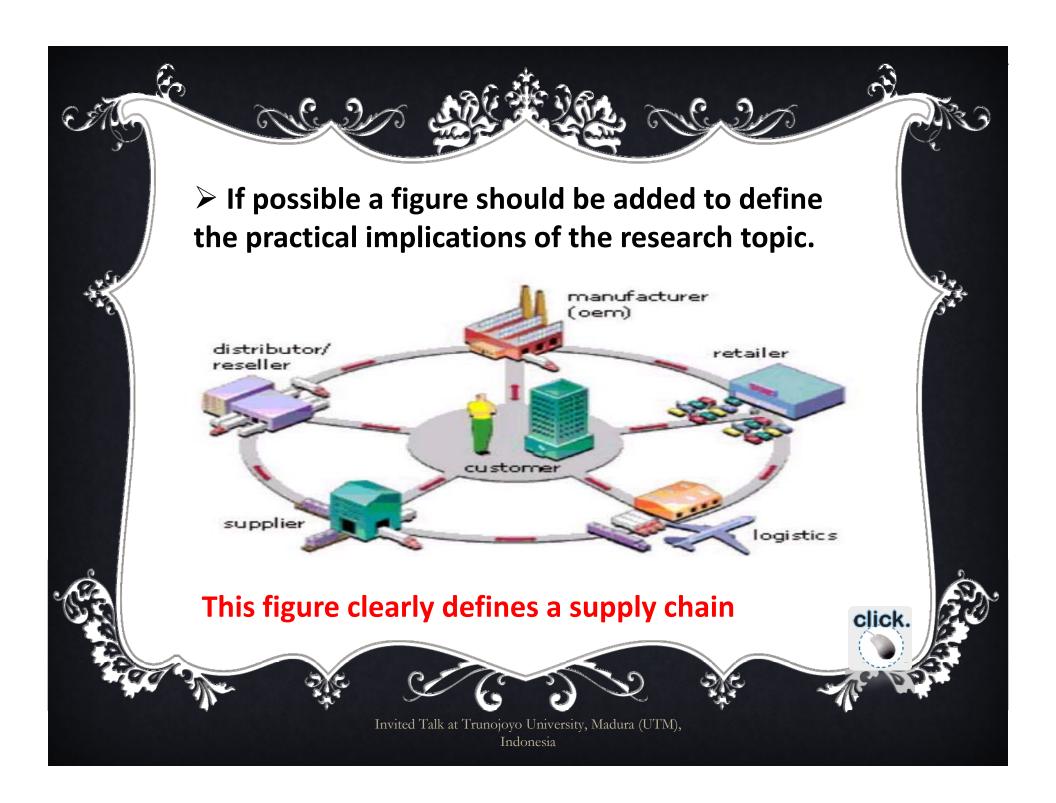


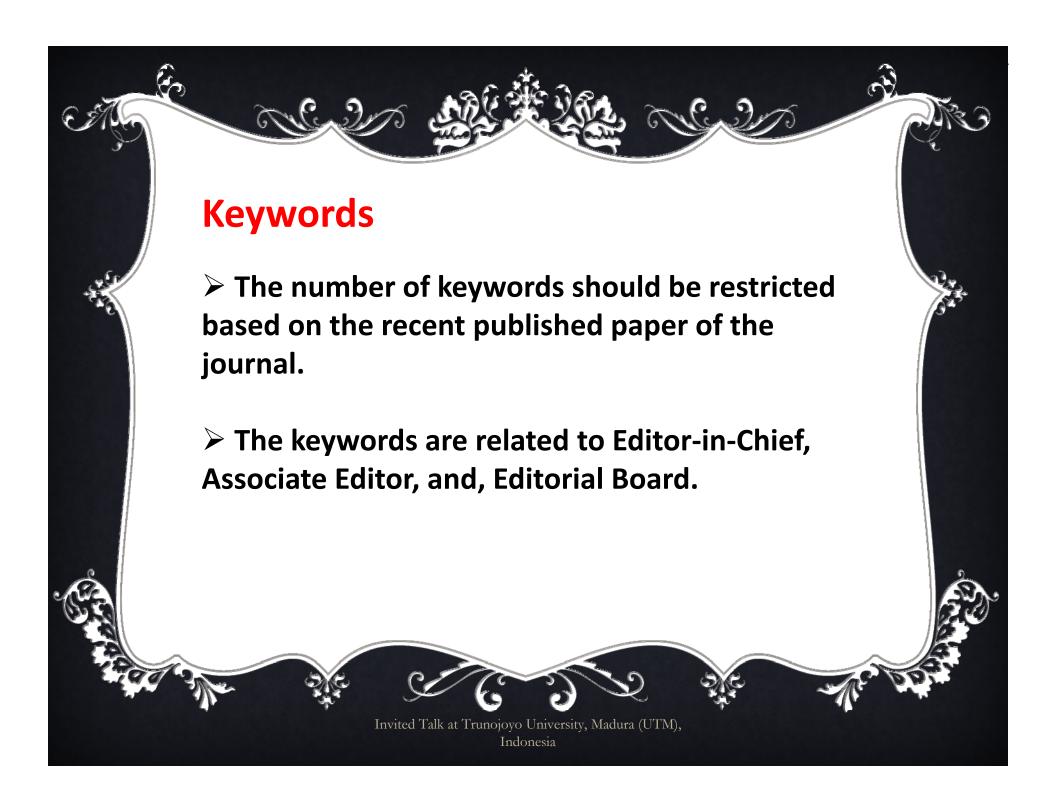
Comparison among the contributions

Table 1. Comparison between the author's contributions.

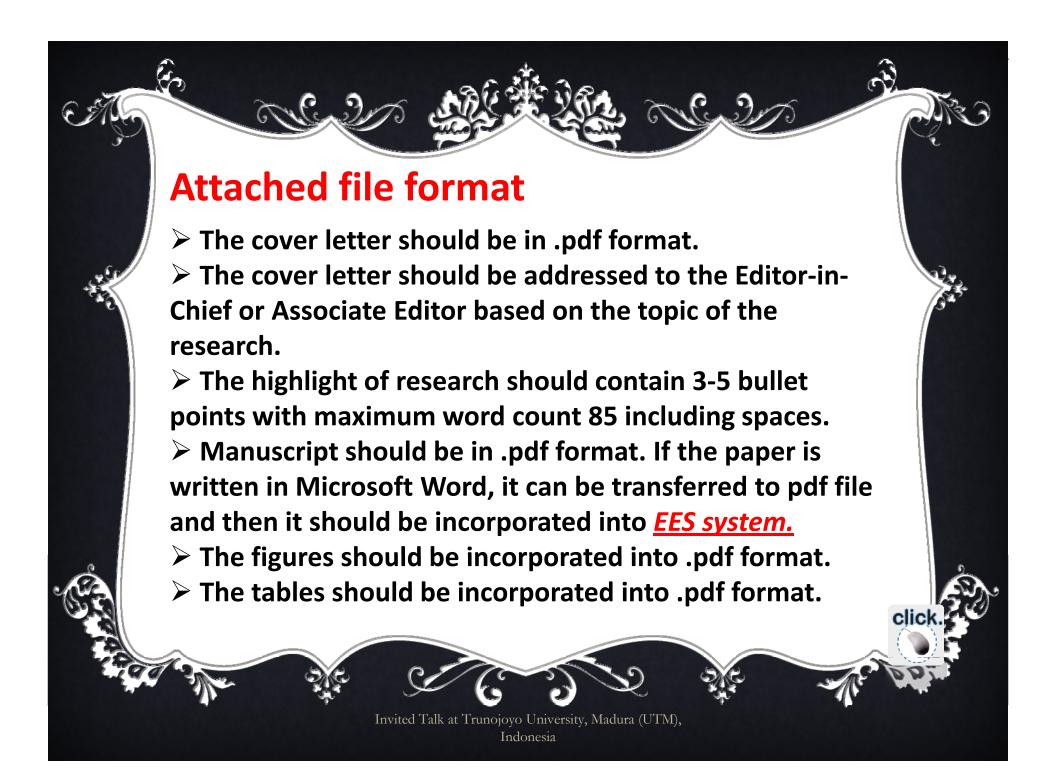
Author(s) Name	Lot size	Number of Deliveries	Reliability	Deterioration	SSMD
Goyal [1]	V	V			
Banerjee [2]	V	V			
Goyal [3]	V	V		V	V
Yang & Wee [4]	V	V			V
Kim & Ha [5]	V	V			V
Yan, Banerjee, and Yang [6]	V	V			V
C'ardenas-	V	V			
Barr'on [7]					
Sarkar&Sarkar				$\sqrt{}$	
[8]					
Sarkar [9]		$\sqrt{}$		$\sqrt{}$	$\sqrt{}$
This paper	$\sqrt{}$		V	$\sqrt{}$	













ARTICLE INFO

ABSTRACT

Keywords: Quadratic demand Product reliability Inflation

No Indentation —>

The paper deals with an economic manufacturing quantity (EMQ) model for time-dependent (quadratic) demand pattern. Every manufacturing sector wants to produce perfect quality items. But in long run process, there may arise different types of difficulties like labor problem, machinery capabilities problems, etc., due to that the machinery systems shift from in-control state to out-of-control state as a result the manufacturing systems produce imperfect quality items. The imperfect items are reworked at a cost to become the perfect one. The rework cost may be reduced by improvements in product reliability i.e., the production process depend on time and also the reliability parameter. We want to determine the optimal product reliability and production rate that achieves the biggest total integrated profit for an imperfect manufacturing process using Euler-Lagrange theory to build up the necessary and sufficient conditions for optimality of the dynamic variables. Finally, a numerical example is discussed to test the model which is illustrated graphically also.

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1. Introduction

Supply chain management (SCM) is a collaboration among suppliers, manufacturers, retailers, and customers. The supply chain model is used to minimize the total cost or to maximize the total profit throughout the network under the condition that demands of each facilities have to be met. Thus, the integrated inventory control policy is a matter of concern (for ilectances Villa [1], Yang and Wee [2], Viswanathan [3], and Bylka [4]). Goyal [5] developed the first research work on the integrated vendor-buyer problem. Banerjee [6] extended Goyal's [5] model with an assumption on the number of lot size. Goyal [7] extended Banerjee's [6] model by assuming the manufacturing quantity of the vendor as an integer multiple of the buyer's ordering quantity. Huang [8] developed an integrated vendor-buyer model in an imperfect production process. Cárdenas-Barrón [9] made a correction on an inventory model in an imperfect production encourrent pricing and lot sizing for make-to-order contract production. Cárdenas-Barrón et al. [10] used the arithmetic-geometric inequality to solve a vendor-buyer integrated inventory model with a closed form solution.

